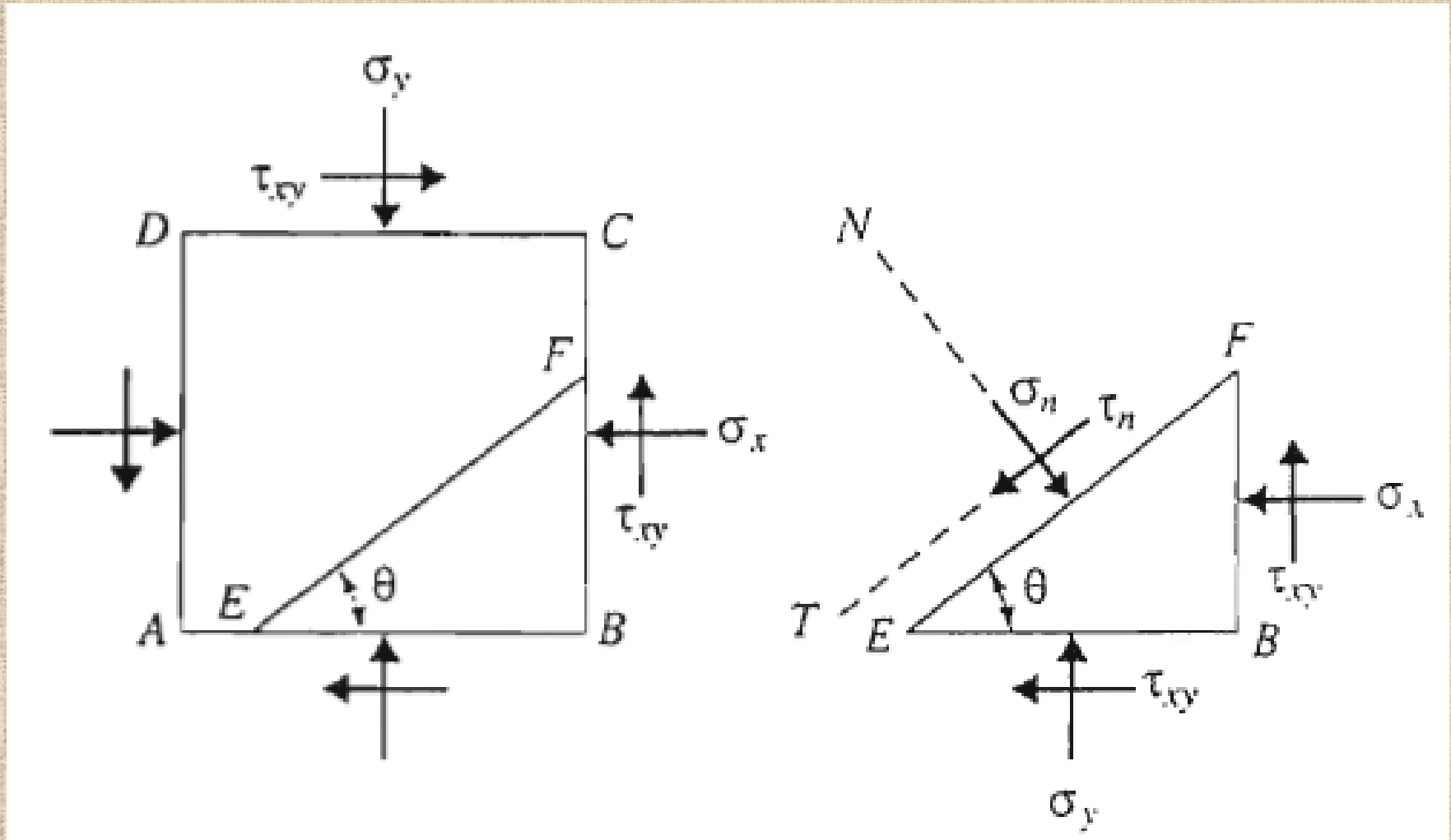


STRESSES IN SOIL MASS (TEGANGAN PADA MASSA TANAH)

PENGERTIAN

- KONTRUKSI PONDASI MENYEBABKAN PERUBAHAN TEGANGAN DALAM TANAH → NET STRESS MENINGKAT
- NILAI NET STRESS TERGANTUNG PADA BEBAN, KEDALAMAN, DAN FAKTOR LAIN
- PENTING UNTUK MENGHITUNG PENINGKATAN TEKANAN INI → PERHITUNGAN PENURUNAN

TEGANGAN NORMAL DAN GESER PADA SUATU BIDANG



TEGANGAN NORMAL DAN GESER PADA SUATU BIDANG

$$\overline{EB} = \overline{EF} \cos \theta$$

$$\overline{FB} = \overline{EF} \sin \theta$$

Summing the components of forces that act on the element in the direction of N and T , we have

$$\sigma_n(\overline{EF}) = \sigma_x(\overline{EF}) \sin^2 \theta + \sigma_y(\overline{EF}) \cos^2 \theta + 2\tau_{xy}(\overline{EF}) \sin \theta \cos \theta$$

or

$$\sigma_n = \sigma_x \sin^2 \theta + \sigma_y \cos^2 \theta + 2\tau_{xy} \sin \theta \cos \theta$$

or

$$\sigma_n = \frac{\sigma_y + \sigma_x}{2} + \frac{\sigma_y - \sigma_x}{2} \cos 2\theta + \tau_{xy} \sin 2\theta$$

TEGANGAN NORMAL DAN GESER PADA SUATU BIDANG

$$\begin{aligned}\tau_n(\overline{EF}) &= -\sigma_x(\overline{EF}) \sin \theta \cos \theta + \sigma_y(\overline{EF}) \sin \theta \cos \theta \\ &\quad - \tau_{xy}(\overline{EF}) \cos^2 \theta + \tau_{xy}(\overline{EF}) \sin^2 \theta\end{aligned}$$

OR

$$\tau_n = \sigma_y \sin \theta \cos \theta - \sigma_x \sin \theta \cos \theta - \tau_{xy}(\cos^2 \theta - \sin^2 \theta)$$

OR

$$\tau_n = \frac{\sigma_y - \sigma_x}{2} \sin 2\theta - \tau_{xy} \cos 2\theta$$

$$\tan 2\theta = \frac{2\tau_{xy}}{\sigma_y - \sigma_x}$$

TEGANGAN NORMAL DAN GESER PADA SUATU BIDANG

Major principal stress:

$$\sigma_n = \sigma_1 = \frac{\sigma_y + \sigma_x}{2} + \sqrt{\left[\frac{(\sigma_y - \sigma_x)}{2}\right]^2 + \tau_{xy}^2}$$

Minor principal stress:

$$\sigma_n = \sigma_3 = \frac{\sigma_y + \sigma_x}{2} - \sqrt{\left[\frac{(\sigma_y - \sigma_x)}{2}\right]^2 + \tau_{xy}^2}$$

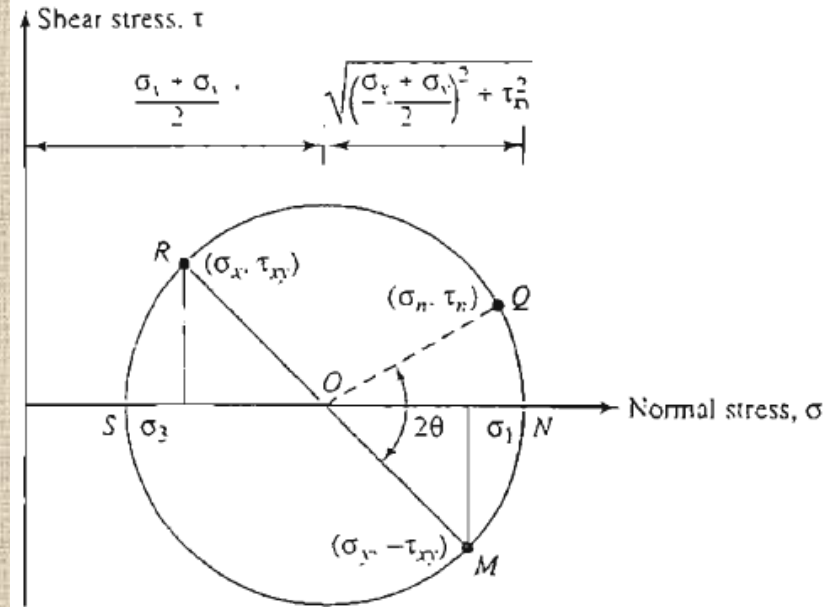


Figure 9.2 Principles of the Mohr's circle

TEGANGAN NORMAL DAN GESER PADA SUATU BIDANG

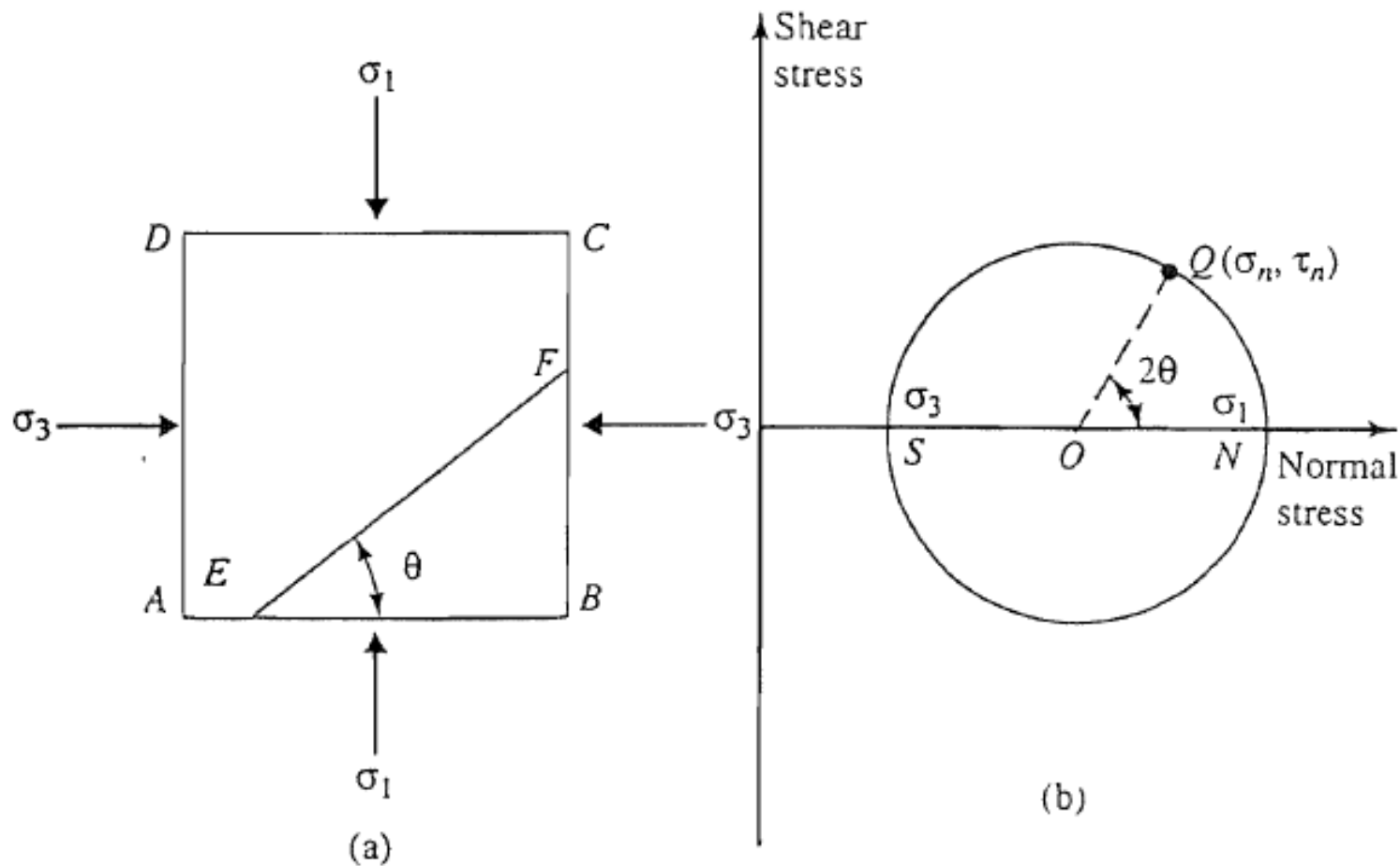


Figure 9.3 (a) Soil element with AB and AD as major and minor principal planes; (b) Mohr's circle for soil element shown in (a)

CONTOH

A soil element is shown in Figure 9.4. The magnitudes of stresses are $\sigma_x = 120 \text{ kN/m}^2$, $\tau = 40 \text{ kN/m}^2$, $\sigma_y = 300 \text{ kN/m}^2$, and $\theta = 20^\circ$. Determine

- Magnitudes of the principal stresses
- Normal and shear stresses on plane AB . Use Eqs. (9.3), (9.4), (9.6), and (9.7).

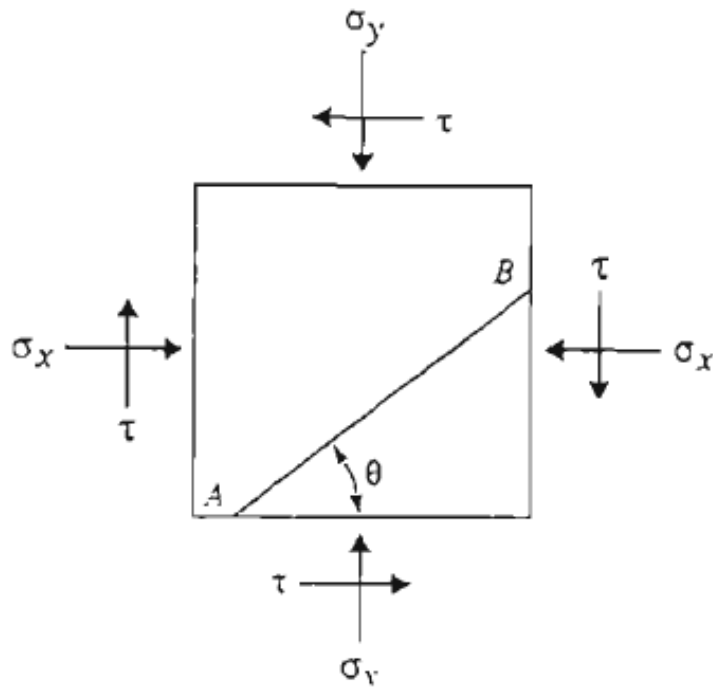


Figure 9.4 Soil element with stresses acting on it

CONTOH

Solution

a. From Eqs. (9.6) and (9.7),

$$\left. \begin{array}{l} \sigma_3 \\ \sigma_1 \end{array} \right\} = \frac{\sigma_y + \sigma_x}{2} \pm \sqrt{\left[\frac{\sigma_y - \sigma_x}{2} \right]^2 + \tau_{xy}^2}$$
$$= \frac{300 + 120}{2} \pm \sqrt{\left[\frac{300 - 120}{2} \right]^2 + (-40)^2}$$

$$\sigma_1 = 308.5 \text{ kN/m}^2$$

$$\sigma_3 = 111.5 \text{ kN/m}^2$$

b. From Eq. (9.3),

$$\sigma_n = \frac{\sigma_y + \sigma_x}{2} + \frac{\sigma_y - \sigma_x}{2} \cos 2\theta + \tau \sin 2\theta$$
$$= \frac{300 + 120}{2} + \frac{300 - 120}{2} \cos (2 \times 20) + (-40) \sin (2 \times 20)$$
$$= 252.23 \text{ kN/m}^2$$

CONTOH

From Eq. (7.4),

$$\begin{aligned}\tau_n &= \frac{\sigma_y - \sigma_x}{2} \sin 2\theta - \tau \cos 2\theta \\ &= \frac{300 - 120}{2} \sin (2 \times 20) - (-40) \cos (2 \times 20) \\ &= 88.49 \text{ kN/m}^2\end{aligned}$$