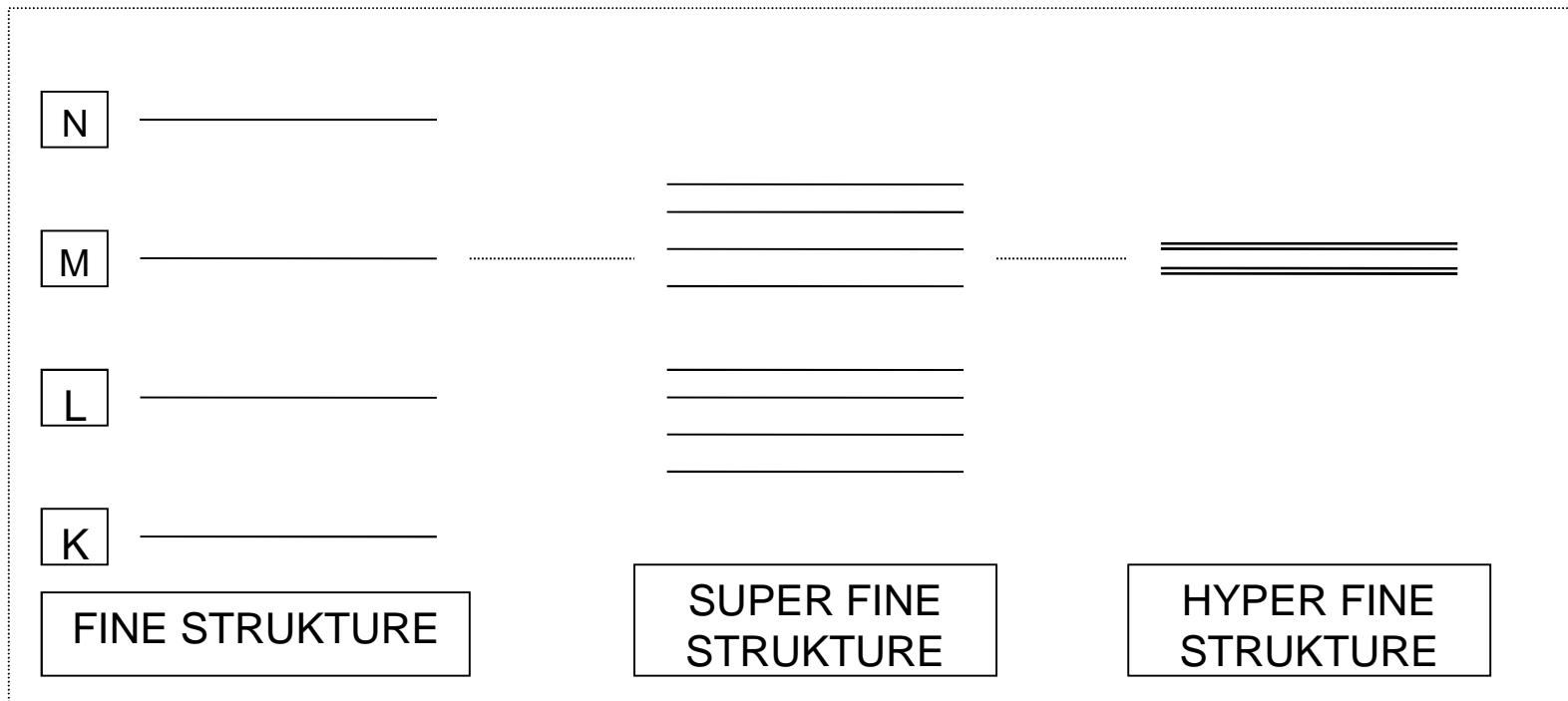


ELEKTRON SPIN

BUKTI EKSPERIMENT TENTANG ADANYA SPIN FINE STRUKTURE



KULIT	K	K	L	M	N
n	:	1	2	3	4
l	:	0	0,1	...	(n-1)
s	:	$\frac{1}{2}, -\frac{1}{2}$			\vec{S}

$$\begin{aligned}\vec{J} &= \vec{L} + \vec{S} \\ |\vec{J}| &+ |l+s| \dots |l+s-1| \\ \dots &|l-s|\end{aligned}$$

Contoh : Kulit M $n = 3, l = 0,1,2$

$$l=0 \Rightarrow |\vec{J}| = \frac{1}{2} \Rightarrow m_s = -\frac{1}{2}, +\frac{1}{2}$$

$$l=1 \Rightarrow |\vec{J}| = \frac{3}{2} \Rightarrow m_s = -\frac{3}{2}, -\frac{1}{2} + \frac{1}{2}, \frac{3}{2}$$

$$l=2 \Rightarrow |\vec{J}| \begin{cases} = \frac{1}{2} \Rightarrow m_s = -\frac{1}{2}, \frac{1}{2} \\ = \frac{5}{2} \Rightarrow m_s = -\frac{5}{2}, -\frac{3}{2}, -\frac{1}{2} + \frac{1}{2}, \frac{3}{2}, \frac{5}{2} \\ = \frac{3}{2} \Rightarrow m_s = -\frac{3}{2}, -\frac{1}{2} + \frac{1}{2}, \frac{3}{2} \end{cases}$$

$$l=0 \ (s) \quad j=\frac{1}{2} \Rightarrow m_s=2e$$

$$l=1 \ (p) \quad j=\frac{1}{2} \Rightarrow m_s=2e$$

$$l=1 \ (p) \quad j=\frac{3}{2} \Rightarrow m_s=4e$$

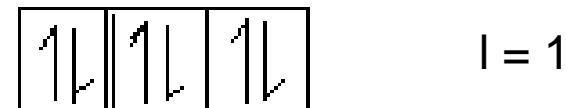
$$l=2 \ (d) \quad j=\frac{3}{2} \Rightarrow m_s=4e$$

$$l=2 \ (d) \quad j=\frac{5}{2} \Rightarrow m_s=6e$$

$S = \text{bulat} \Rightarrow \text{partikel boson}$

$$S=\frac{1}{2}, \text{bilangan ganjil} \Rightarrow \text{fermion} \quad J=\frac{1}{2} \quad l=0$$

$$J=\frac{1}{2} \quad l=0 \quad \begin{matrix} 3 \\ \vdots \end{matrix}$$



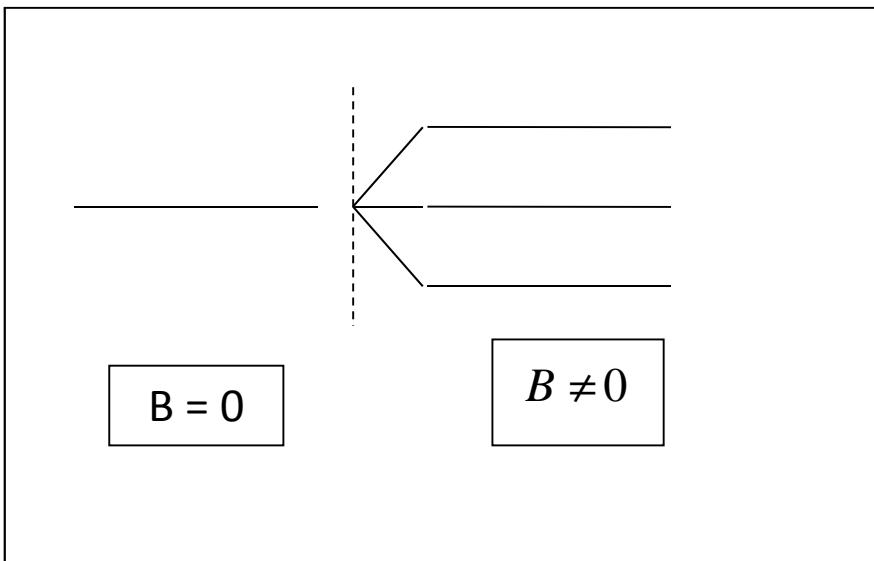
$$J=\frac{3}{2} \quad J=\frac{5}{2}$$



$$l=2$$



ANOMALI EFEK ZEEMAN



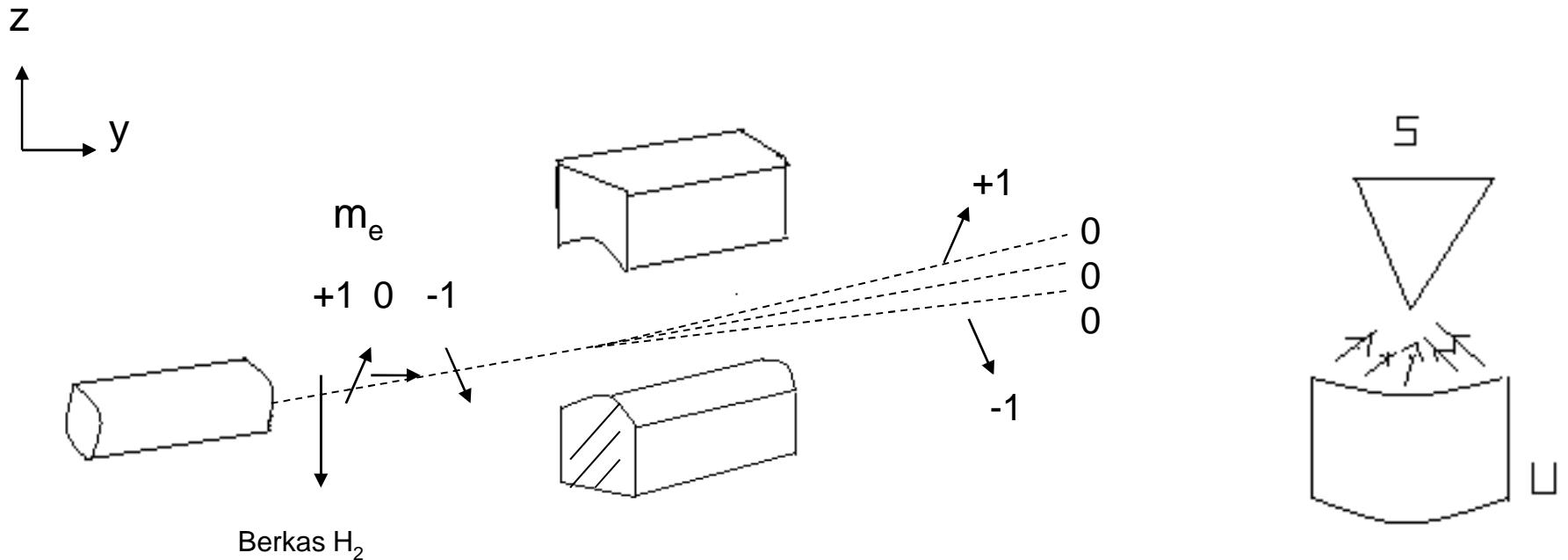
Untuk $Z = \text{genap} \Rightarrow$ benar atom akan pecah masuk ke medan B sejumlah bil. Ganjil memperkuat asumsi bahwa $I = \text{bulat}$ (efek zeeman normal).

Ganjil \Rightarrow atom pecah bil. Genap $\Rightarrow I = \text{bulat}$.

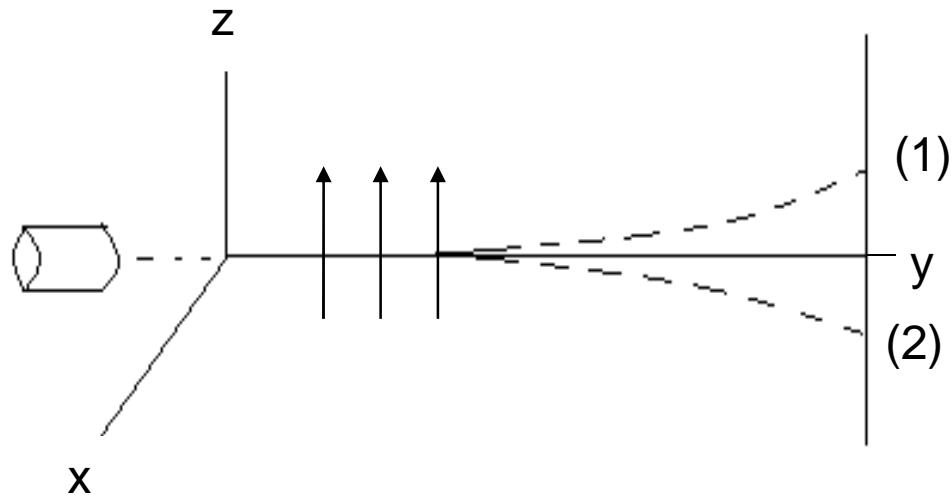
Tak normal \Rightarrow anomali

Dipengaruhi $\vec{B} = \text{efek zeeman}$

$E = \text{efek Strake}$



Seberkas atom dilewatkan dalam daerah yang terdapat \vec{B} ($B_z \hat{z}$). Atom-atom dengan arah momen dipole berlawanan mengalami gaya dalam dua arah yang berlawanan.



$$\vec{M} = \frac{\mu B}{\hbar} \vec{L} \quad \text{dimana}$$

$$\mu = \text{Magneton Bohr} = \frac{q\hbar}{2m_e}$$

\vec{M} = momen dipole magnet

\vec{L} = momentum sudut orbital

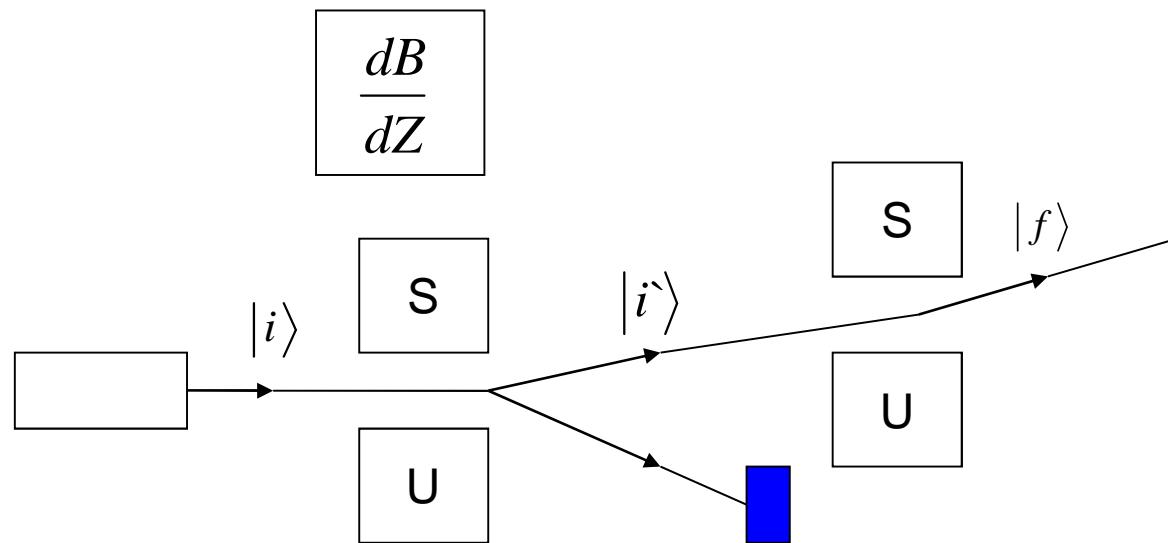
ANALISIS PERCOBAAN STERN GERLACH

$$|1\rangle = |S_z = +\rangle ; |2\rangle = |S_z = -\rangle$$

$$|i\rangle = a|S_z = +\rangle + b|S_z = -\rangle$$

$$\langle + | i \rangle = a \langle + | + \rangle + b \langle + | - \rangle = 1$$

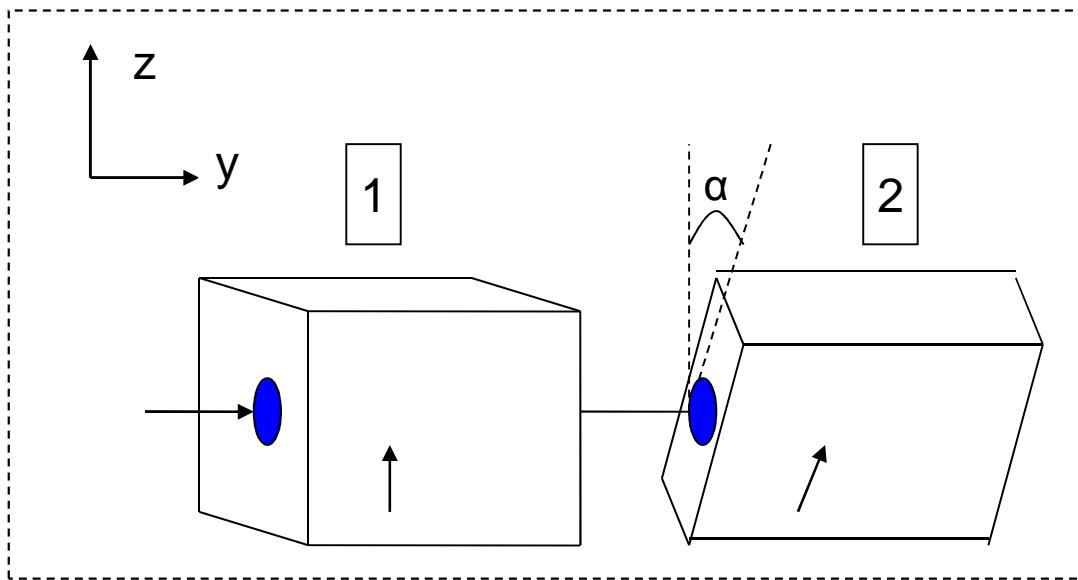
$$\langle - | i \rangle = a \langle - | + \rangle + b \langle - | - \rangle = 1$$



$$|\langle + | i \rangle|^2 = |\langle - | i \rangle|^2 \Leftrightarrow \langle + | i \rangle \langle + | i \rangle^* + \langle - | i \rangle \langle - | i \rangle^*$$

Bagaimana jika divais SG yang kedua membentuk sudut α dengan yang pertama?

FILTER STERN GERLACH



untuk $\alpha=90$

$z \Leftrightarrow x$

$$|S_x = \pm\rangle \neq |S_z = \pm\rangle$$

$$\text{filter}(1)|S_z = +\rangle, \text{filter}(2) = |S_x = -\rangle$$

$$\langle S_x = + | S_z = + \rangle \neq 0 \text{ dan}$$

$$\langle S_x = - | S_z = + \rangle \neq 0$$

$$\langle S_z = + | S_x = - \rangle \langle S_x = - | S_z = + \rangle + \langle S_z = - | S_x = - \rangle \langle S_x = - | S_z = + \rangle$$

OPERATOR DAN MATRIKS

Berkas electron mula-mula $|i\rangle$ melewati divais SG menjadi $|f\rangle$. Amplitude proses $\langle f | A | i \rangle$;
A = operator sebagai representasi proses dalam divais SG

$$\langle f | A | i \rangle = \sum_{\alpha, \beta} \langle f | \alpha \rangle \langle \alpha | A | \beta \rangle \langle \beta | i \rangle$$

$\langle \alpha | A | \beta \rangle$ dengan element matriks A

$$\begin{array}{cc} |S_z=+\rangle & |S_z=-\rangle \\ \hline |S_z=+\rangle & \begin{pmatrix} \langle S_z=+|A|S_z=+ \rangle & \langle S_z=+|A|S_z=- \rangle \\ \langle S_z=-|A|S_z=+ \rangle & \langle S_z=-|A|S_z=- \rangle \end{pmatrix} \begin{bmatrix} \frac{\hbar}{2} & 0 \\ 0 & \frac{\hbar}{2} \end{bmatrix} \\ |S_z=-\rangle & \end{array}$$

Matriks S_y dan S_x dan solusi persamaan eigen

$$[S_x, S_y] = \hbar S_z$$

x, y, z silidik

$$|S_x=\pm\rangle = \frac{1}{\sqrt{2}} \{ |S_z=+\rangle \pm |S_z=-\rangle \}$$

$$|S_y=\pm\rangle = \frac{1}{\sqrt{2}} - \{ |S_z=+\rangle \pm i |S_z=-\rangle \}$$

Ruang keadaan spin $|s, m\rangle$ dengan

$$S^2 |s, m\rangle = s(s+1)\hbar^2 |s, m\rangle$$

$$S_z |s, m\rangle = m\hbar |s, m\rangle$$

$$S_+ = S_x + iS_y \quad ; \quad S_- = S_x - iS_y \quad ; \quad \Rightarrow \quad S_x = \frac{1}{2}(S_+ + S_-) \quad ; \quad S_y = \frac{1}{2i}(S_+ - S_-)$$

$$S_x |i\rangle = v |i\rangle \quad \Rightarrow \quad \frac{\hbar}{2} \begin{pmatrix} 0 & 1 \\ 1 & 0 \end{pmatrix} \begin{pmatrix} a \\ b \end{pmatrix} = \lambda \begin{pmatrix} a \\ b \end{pmatrix}$$

$$\begin{bmatrix} -\frac{2\lambda}{\hbar} & 0 \\ 0 & -\frac{2\lambda}{\hbar} \end{bmatrix} = 0 \Rightarrow v = \pm \frac{\hbar}{2} \quad \rightarrow a = b = \frac{1}{\sqrt{2}} \quad a = -b = -\frac{1}{\sqrt{2}}$$

$$+\frac{1}{2} \frac{\hbar}{2} \quad \text{dan} \quad -\frac{1}{2} \frac{\hbar}{2} \quad \rightarrow \quad \text{nilai eigen}$$

$$\begin{pmatrix} \frac{1}{\sqrt{2}} \\ \frac{1}{\sqrt{2}} \end{pmatrix} \text{ dan } \begin{pmatrix} -\frac{1}{\sqrt{2}} \\ \frac{1}{\sqrt{2}} \end{pmatrix} \rightarrow \text{spinor eigen}$$

MATRIKS PAULI

$$S_x = \frac{1}{2}\hbar\sigma_x \quad : \quad S_y = \frac{1}{2}\hbar\sigma_y \quad : \quad S_z = \frac{1}{2}\hbar\sigma_z \quad dengan$$

$$\sigma_x = \begin{pmatrix} 0 & 1 \\ 1 & 0 \end{pmatrix} ; \quad \sigma_y = \begin{pmatrix} 0 & -i \\ 1 & 0 \end{pmatrix} ; \quad \sigma_z = \begin{pmatrix} 1 & 0 \\ 0 & -1 \end{pmatrix}$$

$$\sigma_i^2 = I \quad ; \quad \sigma_i\sigma_j + \sigma_j\sigma_i = 2\sigma_{ij}I \quad ; \quad [\sigma_x, \sigma_y] = 2i\sigma_z$$

$$\vec{S} = \hbar \frac{\vec{\sigma}}{2} \rightarrow \sigma^2 = 3 \rightarrow S^2 = \frac{\hbar^2 \sigma^2}{4} = s(s+1)\hbar^2 = \frac{3}{4}\hbar^2$$

TRANSFORMASI MATRIKS

Satu filter SG disusun dalam keadaan $|S_z = \alpha\rangle$ yang lain diukur sehingga $|\langle S_y = i | S_z = \alpha \rangle|^2$ mendapatkan berkas keadaan S_y . semua data exp. yang mungkin diberikan oleh element-element yang dinamakan matrik transformasi.